

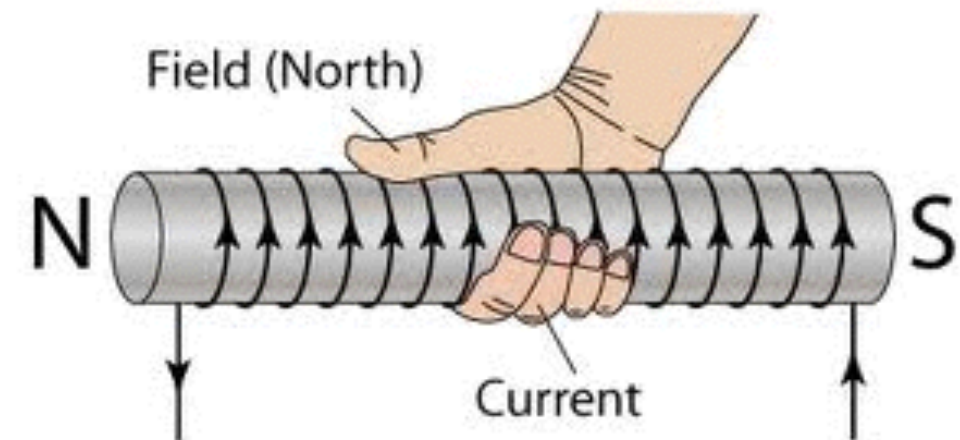
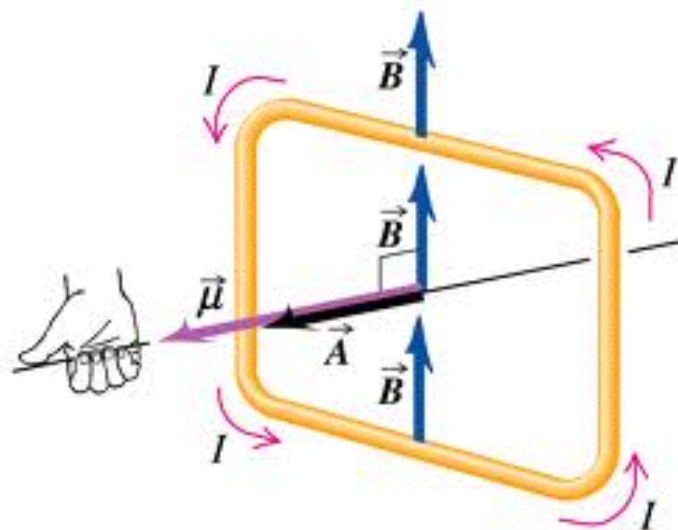
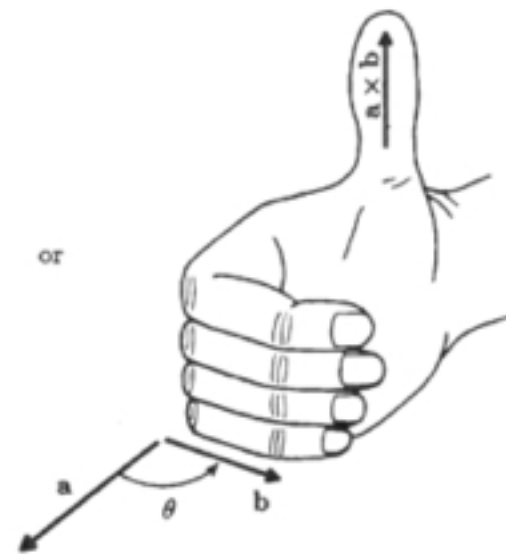
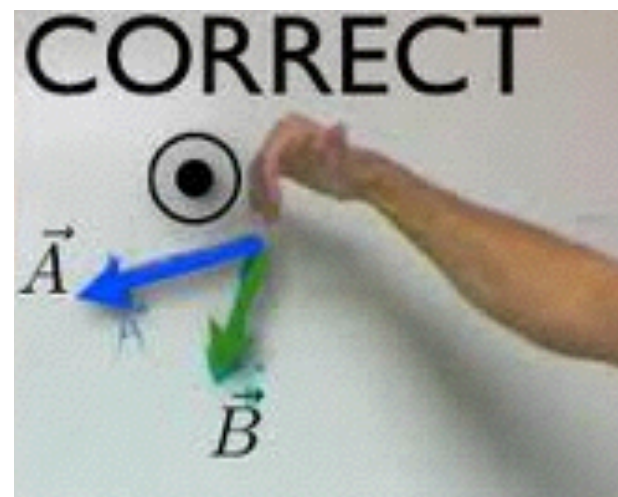
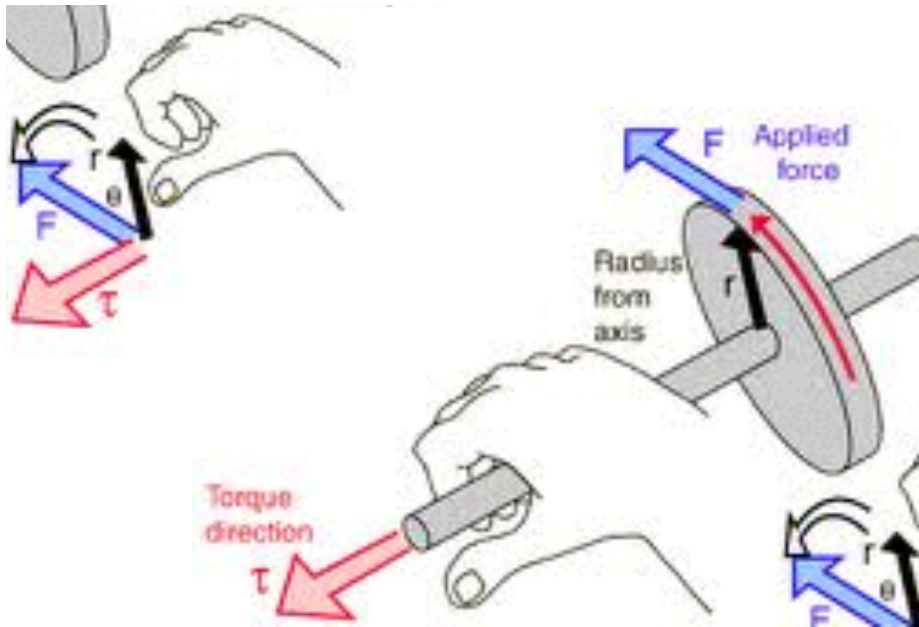
Ampère Law

Lecture 20

Announcements

- Reading for Wednesday: 28-1 to 28-3

Review: Right Hand Rules



Aside...

- Electric Constant (**Permittivity** of free space):

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2$$

- Magnetic Constant (**Permeability** of free space):

$$\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m}/\text{A}$$

Just for fun clicker...

Railgun

From Wikipedia, the free encyclopedia

For railroad artillery, see [Railway gun](#). For other uses, see [Rail-gun \(disambiguation\)](#).

See also: [Coilgun](#)

A **railgun** is an [electrically powered](#) electromagnetic projectile launcher based on similar principles to the [homopolar motor](#). A railgun comprises a pair of parallel conducting rails, along which a sliding [armature](#) is accelerated by the electromagnetic effects of a current that flows down one rail, into the armature and then back along the other rail.^[2]

Railguns are being researched as a weapon with a [projectile](#) that would not use explosives nor propellant, but rather rely on electromagnetic forces to achieve a very high [kinetic energy](#), somewhat similar to a [kinetic energy penetrator](#). While current kinetic energy penetrators such as an [armour-piercing fin-stabilized discarding-sabot](#) can achieve a [muzzle velocity](#) on the order of [Mach 5](#), railguns can potentially exceed Mach 10, and thus far exceed conventionally delivered munitions in range and destructive force, with the absence of explosives to store and handle as an additional advantage. Railguns have long existed as experimental technology but the mass, size and cost of the required power supplies have prevented railguns from becoming practical military weapons. However, in recent years, significant efforts have been made towards their development as feasible military technology. For example, in the late 2000s, the [U.S. Navy](#) tested a railgun that accelerates a 3.2 kg (7 pound) projectile to [hypersonic](#) velocities of approximately 2.4 kilometres per gave the project the [Latin](#) motto "Velocitas Eradico", Latin for "I, [who am] speed, eradicate".

In addition to military applications, NASA has proposed to use a railgun from a high-altitude aircraft to fire a small [forces](#) involved would necessarily restrict the usage to only the sturdiest of payloads.



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Review: Fundamental law(s) of Electrostatics

- **Coulomb Law:** (Solution to DE) E field generated by charge

$$\vec{E} = \frac{kq}{r^2} \hat{r} \qquad d\vec{E} = \frac{dq}{4\pi\epsilon_0} \frac{\hat{r}}{r^2}$$

or

Gauss Law: (DE) Relationship between charge of E field

Integral Equation:

$$\oint_{\mathcal{M}} d^2A \, \hat{n} \cdot \vec{E} = Q_{\text{inside}}/\epsilon_0$$

Differential Equation (DE):

$$\vec{\nabla} \cdot \vec{E} = \rho/\epsilon_0$$

Review: Fundamental law(s) of B field generation

Biot-Savart Law: (Solution to DE) B generated by current:

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{\ell} \times \hat{r}}{r^2}$$

or

Ampère Law: (DE) Relationship between current and B field

Integral Equation:

$$\oint d\vec{\ell} \cdot \vec{B} = \mu_0 I_{\text{inside}}$$

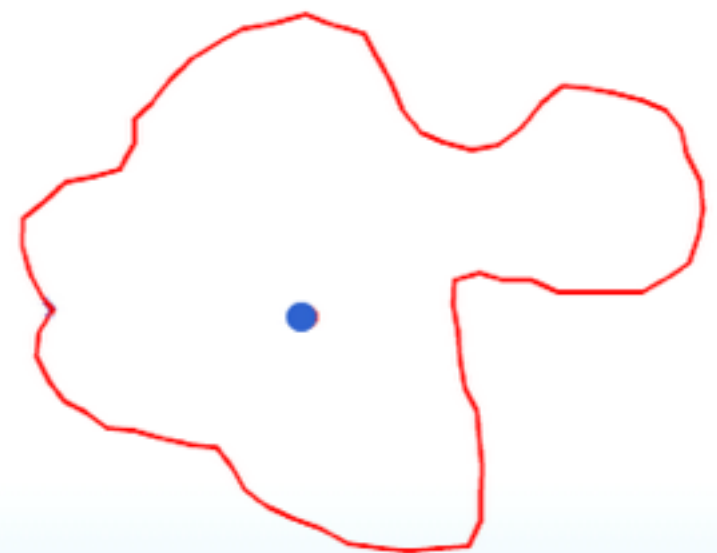
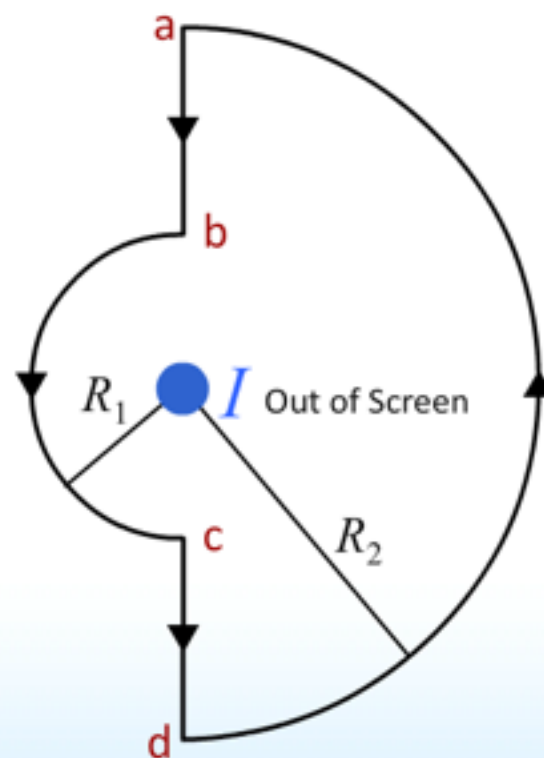
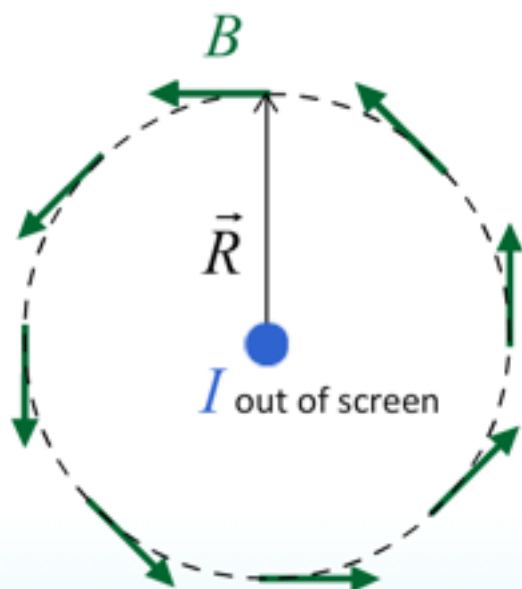
Differential Equation (DE):

$$\vec{\nabla} \times \vec{B} = \mu_0 \vec{j}$$

Ampère Law

- New physical law (same physics as Biot-Savart)
- Line integral over a closed loop:

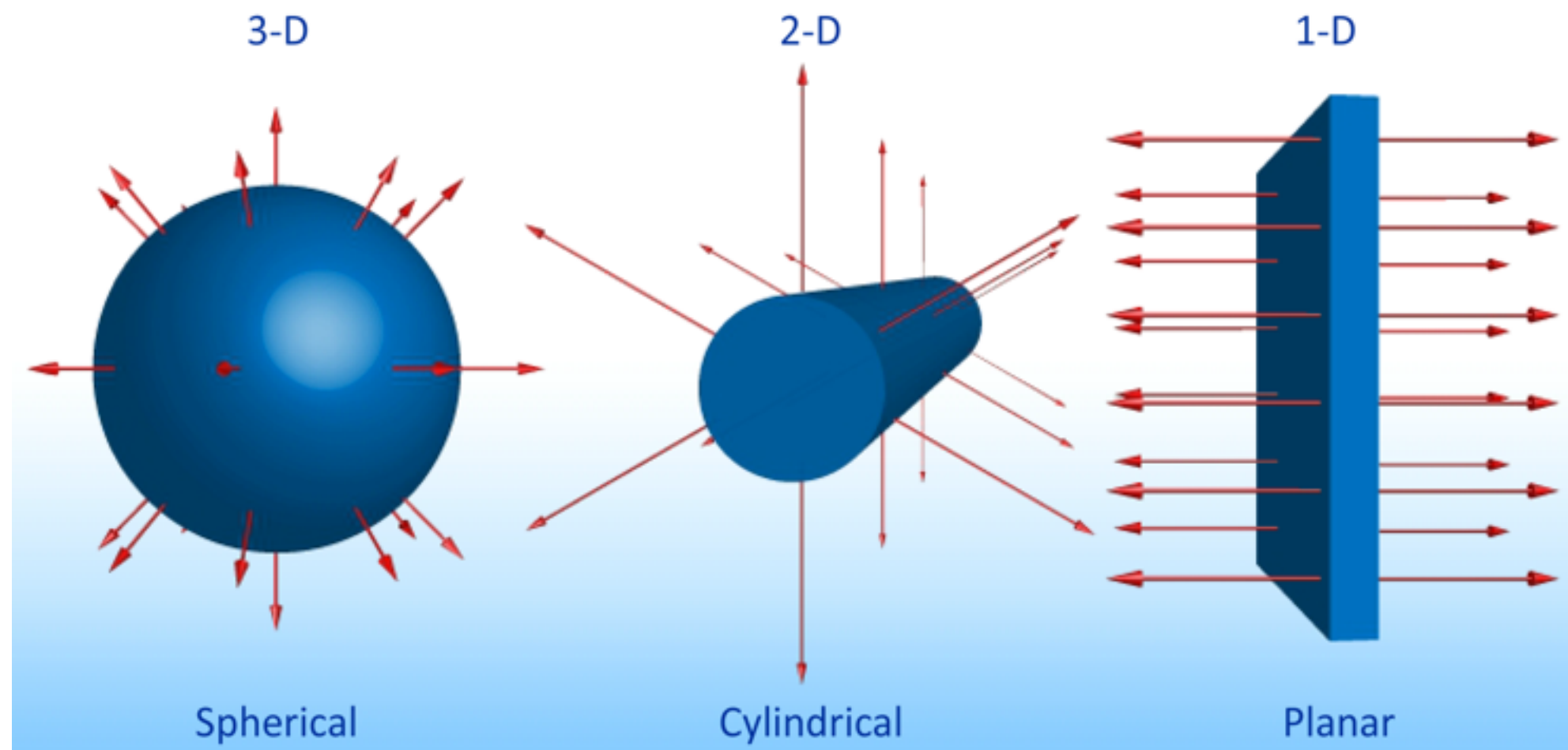
$$\oint \vec{d\ell} \cdot \vec{B} = \mu_0 I_{\text{inside}}$$



Review: Gauss Law and computing E

$$\oint d^2A \hat{n} \cdot \vec{E} = \frac{Q_{\text{enclosed}}}{\epsilon_0}$$

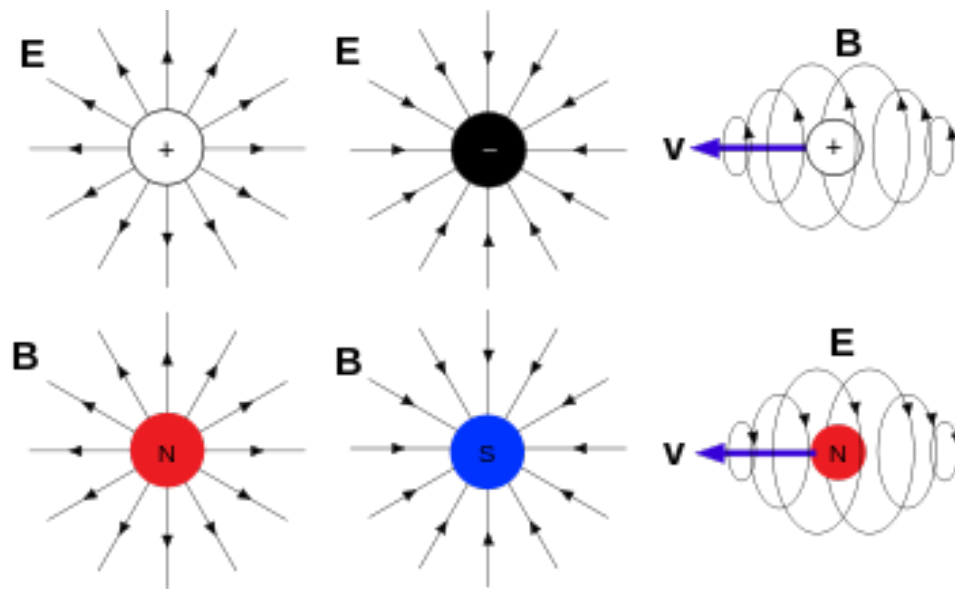
Special Symmetries



By the way: Gauss Law for B

- No magnetic monopoles (except on 2/14 ❤️)

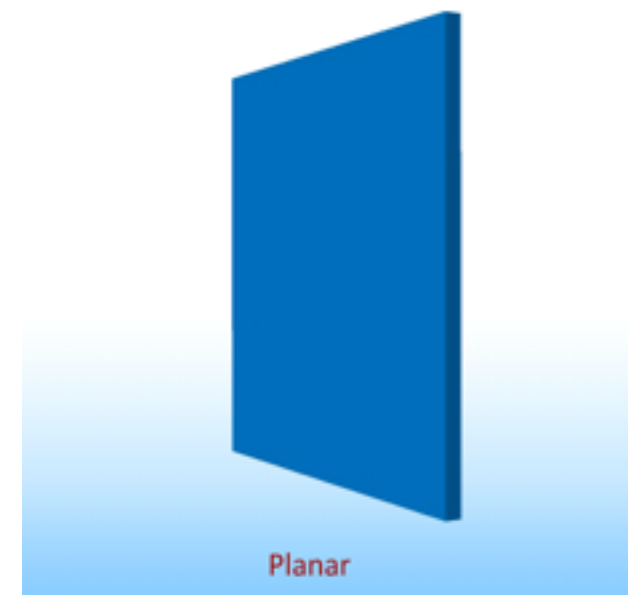
$$\oint d^2A \hat{n} \cdot \vec{B} = \frac{Q_{\text{enclosed}}^M}{\epsilon_0^M} = 0$$



New: Ampère Law and computing B

$$\oint \vec{d\ell} \cdot \vec{B} = \mu_0 I_{\text{inside}}$$

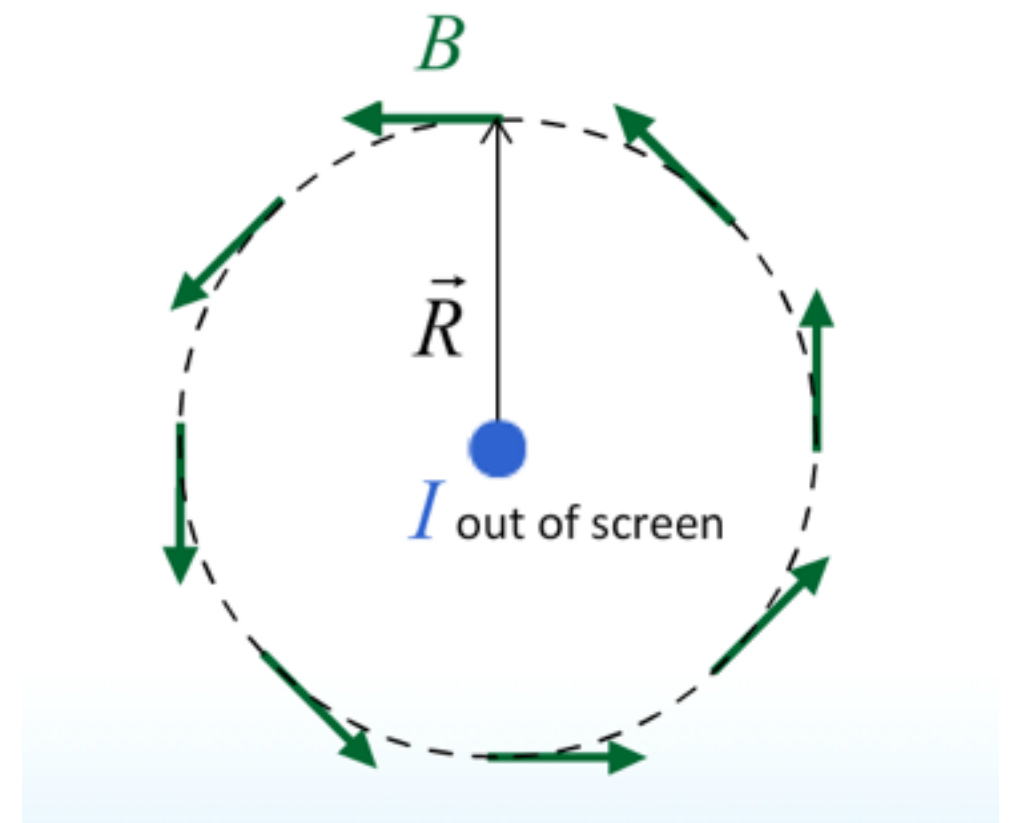
1. Identify **symmetry** (only 2 options)
2. Draw B field/field lines
3. Choose a Ampère Loop
4. Compute B



Ampère Law: Infinite Wire (1)

(Overhead)

1. Identify **symmetry**
2. Draw B field/field lines
3. Choose a Ampère Loop
4. Compute B

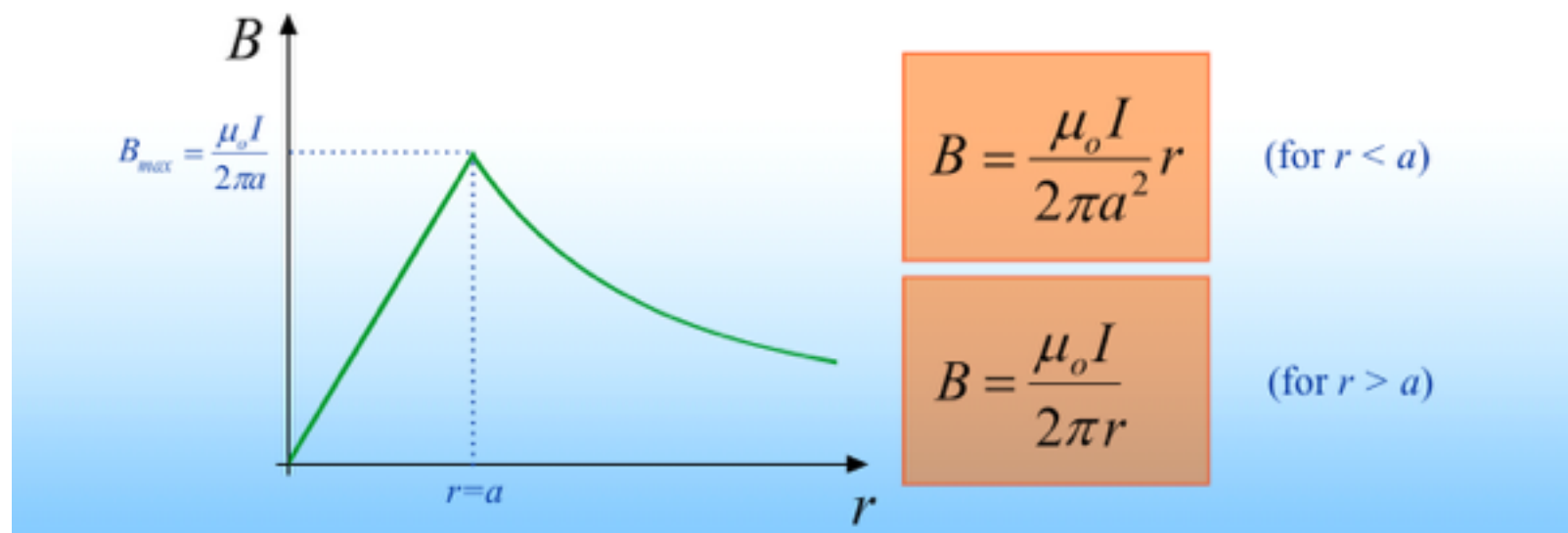
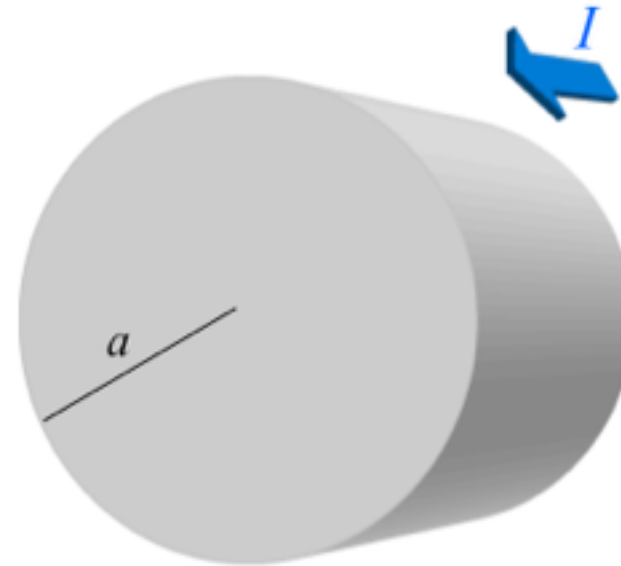


$$B = \frac{\mu_0 I}{2\pi R}$$

Ampère Law: Infinite Wire (2)

(Overhead)

- Why is n const?
- Why must wire be infinite?

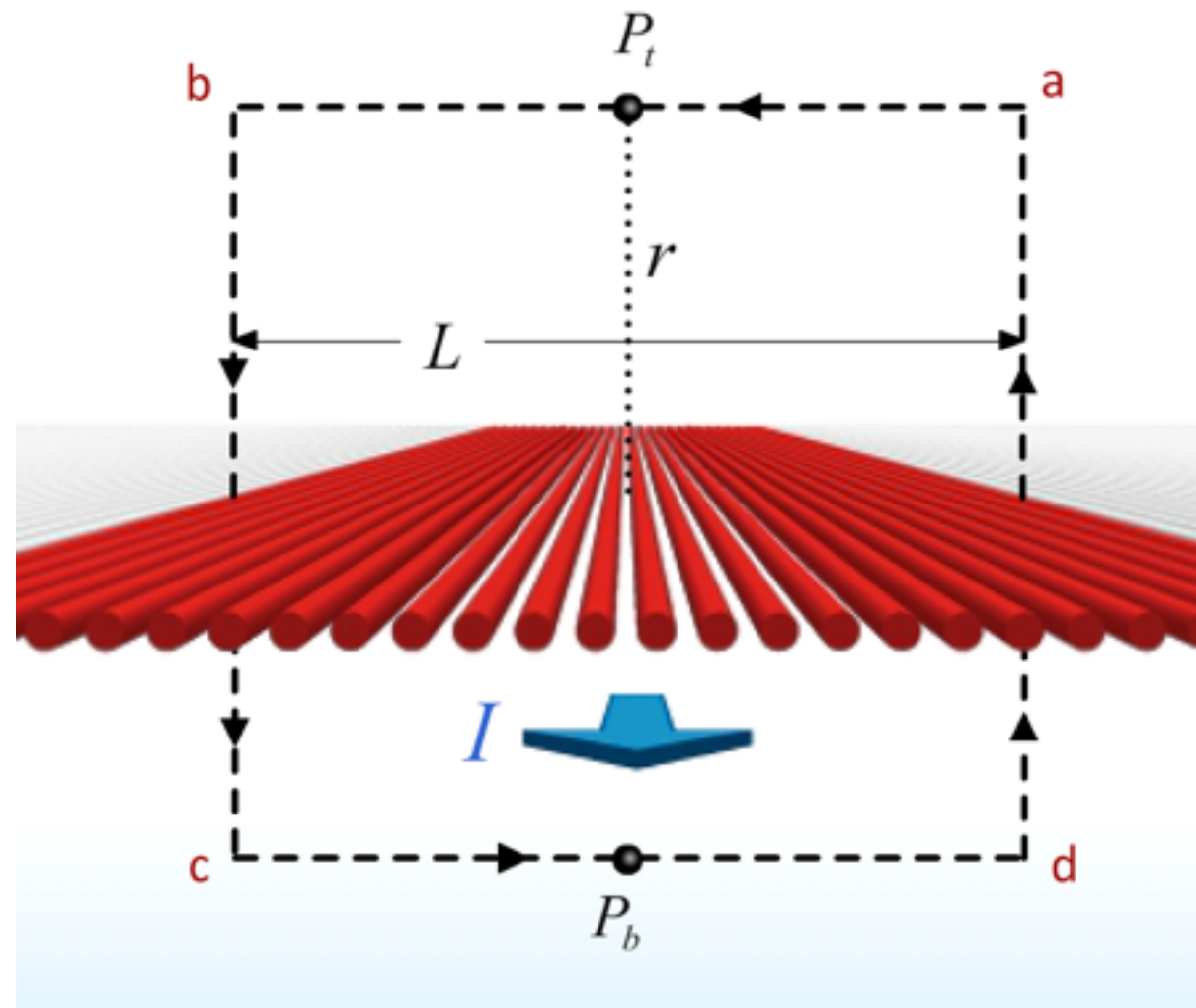


Clicker...

Ampère Law: Infinite Sheet

(Overhead)

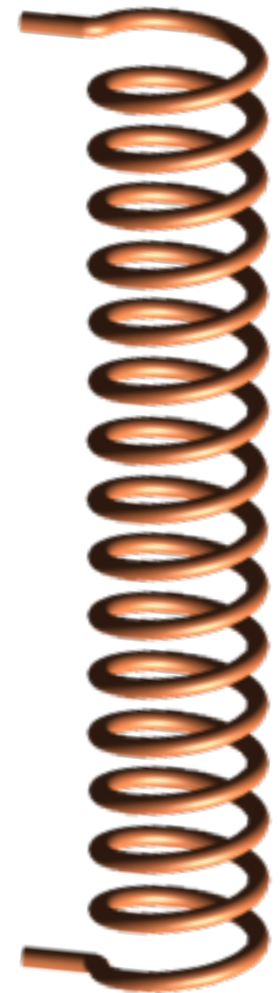
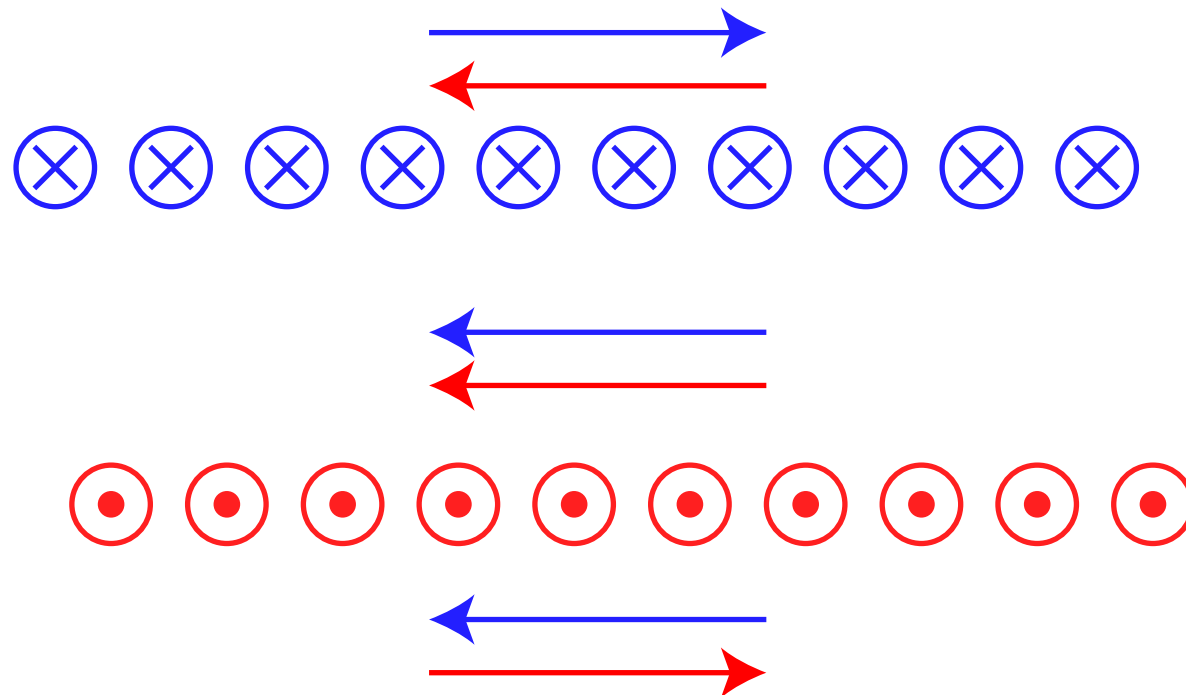
1. Identify **symmetry**
2. Draw B field/field lines
3. Choose a Ampère Loop
4. Compute B



$$B = \frac{1}{2} \mu_0 n I$$

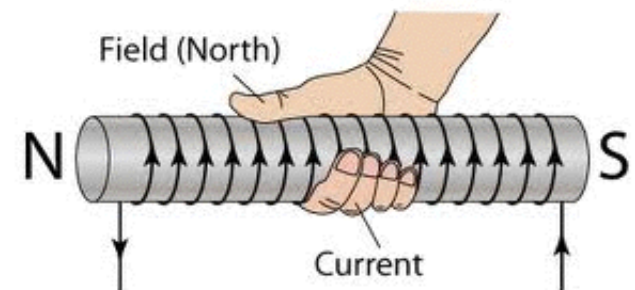
B field for an ∞ solenoid

- Intuitive picture: \sim 2 infinite sheets



- Field is \sim zero outside

$$B = \mu_0 n I$$



Electrodynamics & the Maxwell Equations

- Gauss Law (E): $\oint_{\mathcal{M}} d^2A \hat{n} \cdot \vec{E} = Q_{\text{inside}}/\epsilon_0$
- Gauss Law (B): $\oint_{\mathcal{M}} d^2A \hat{n} \cdot \vec{B} = 0$
- Ampère Law: $\oint_{\partial\mathcal{M}} \vec{d\ell} \cdot \vec{B} = \mu_0 I + \mu_0\epsilon_0 \frac{d}{dt} \int_{\mathcal{M}} d^2A \hat{n} \cdot \vec{E}$
- Faraday Law: $\oint_{\partial\mathcal{M}} \vec{d\ell} \cdot \vec{E} = -\frac{d}{dt} \int_{\mathcal{M}} d^2A \hat{n} \cdot \vec{B}$