

122 Exam 2 Equations, Tipler Chapters 23-25

Exam 1 equations:

$$e = 1.60 \times 10^{-19} \text{ C} \quad \vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r} \quad \text{Gauss: } \phi_{net} = \oint_S \vec{E} \cdot \hat{n} dA = \frac{Q_{inside}}{\epsilon_0}$$

$$k = \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2 \quad \epsilon_0 = \frac{1}{4\pi k} = 8.85 \times 10^{-12} \text{ C}^2 / (\text{N}\cdot\text{m}^2)$$

$$\infty \text{ line: } E_R = \frac{1}{2\pi\epsilon_0} \frac{\lambda}{R} \quad \infty \text{ plane: } E_z = \text{sign}(z) \cdot \frac{\sigma}{2\epsilon_0} \quad \text{thin sph. shell: } \begin{matrix} E_r = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} & r > R \\ E_r = 0 & r < R \end{matrix}$$

Chapter 23:

$$\text{Define: } \Delta V = V_b - V_a = \frac{\Delta U}{q_0} = -\int_a^b \vec{E} \cdot d\vec{\ell} \quad \text{Coulomb: } V = \frac{kq}{r} \quad (V = 0 \text{ if } r = \infty)$$

$$\text{Point chgs: } V = \sum_{i=1}^n \frac{kq_i}{r_i} \quad \text{Distributed chgs: } V = \int \frac{k dq}{r} \quad E_{tan} = -\frac{dV}{dl} \quad E_x = -\frac{dV}{dx}$$

$$\vec{E} = -\vec{\nabla}V = -\left( \frac{\partial V}{\partial x} \hat{i} + \frac{\partial V}{\partial y} \hat{j} + \frac{\partial V}{\partial z} \hat{k} \right) \quad \text{Potl Energy: } U = q_0 V \quad 2 \text{ pt chgs: } U = \frac{kq_0 q}{r}$$

Electric potential due to a single point charge :  $V = kQ/r$   
(same expression when external to a uniformly charged sphere or spherical shell)

$$\text{Pt Chgs: } U = \frac{1}{2} \sum_{i=1}^n q_i V_i \quad \text{Conductor: } U = \frac{1}{2} QV \quad \text{System of conductors: } U = \frac{1}{2} \sum_{i=1}^n Q_i V_i$$

Chapter 24:

$$\text{Def: } C = \frac{Q}{V} \quad \text{isol. sphere: } C = 4\pi\epsilon_0 R \quad \text{par plate: } C = \frac{\epsilon_0 A}{d} \quad \text{cyl: } C = \frac{2\pi\epsilon_0 L}{\ln(R_2/R_1)}$$

$$U = \frac{1}{2} QV = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} CV^2 \quad u_e = \frac{1}{2} \epsilon_0 E^2 \quad \text{Par: } C_{eq} = C_1 + C_2 + C_3 + \dots$$

$$\text{Ser: } \frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots \quad \text{Dielectric: } E = \frac{E_0}{\kappa} \quad \text{and } C = \kappa C_0$$

Chapter 25:

$$I = \frac{\Delta Q}{\Delta t} \quad I = qnAv_d \quad \vec{J} = qn\vec{v}_d \quad R = \frac{V}{I} \quad R = \rho \frac{L}{A} \quad \text{Ohm: } V = IR, \text{ for } R = \text{const}$$

$$P = IV \quad \text{Resistor: } P = IV = I^2 R = \frac{V^2}{R} \quad \text{Par: } \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots \quad \text{Ser: } R_{eq} = R_1 + R_2 + \dots$$

Kirchhoff: (1) sum of  $\Delta V$ 's around loop = 0. (2) sum of currents in = sum of currents out of junction  
For an RC circuit,  $Q(t) = Q_{max}(1 - e^{-t/\tau})$ .  $\tau = RC$  time constant,  $Q$  is the charge on  $C$ , charging up from zero at  $t = 0$